

Improved Cloud-to-Ground and Intracloud Lightning Detection with the LS7002 Advanced Total Lightning Sensor

Mejora de la nube-tierra y en la nube Detección relámpago con el LS7002 avanzada Sensor total Rayo

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ABSTRACT

The LS7002 detects low frequency electromagnetic signals from lightning discharges in approximately the 1-350 kHz range. The sensor builds upon the digital technology platform of its predecessor, the LS7001, by employing improved embedded software features. This digital processing enhances the sensitivity of the sensor to low-amplitude signals from lightning events. The LS7002 also uses onset corrections that reduce timing error and improve location accuracy by being able to better determine the arrival time of electromagnetic waveforms. In addition, the ability to remove noise from local sources via digital filtering allows for a better signal-to-noise ratio and more flexibility in site selection. These sensor features along with the latest central processor software (the Total Lightning Processor) allow for an enhanced cloud-to-ground flash detection efficiency of 95% and a network median location accuracy of 250 m. Additionally, with network baseline distances (distances between adjacent sensors in a network) of 300-350 km, an intracloud flash detection efficiency of about 50% can be achieved, with detection efficiency increasing for shorter baseline distances. Recently the U.S. National Lightning Detection Network (NLDN) underwent a major update, in which previous generation IMPACT and LS7001 sensors were replaced by the LS7002. As a result of the enhanced features of the LS7002 and the Total Lightning Processor, the location accuracy for cloud-to-ground lightning improved from about 300 m to as good as 200 m within the interior of the network. The detection efficiencies for cloud-to-ground and intracloud lightning flashes within the NLDN are about 95% and 50%, respectively.

Keywords: lightning detection, lightning sensors, location accuracy, detection efficiency, LS7002

RESUMEN

Se introduce el sensor LS7002 de rayo de baja frecuencia. Resultados de la validación se comparten de la Red Nacional de Detección de Relámpagos en los Estados Unidos. Ubicación precisiones han mejorado al mejor de 200 metros y en la nube de detección de rayos es cercana al 50%.

Palabras clave: detección de rayos, sensores de rayos, precisión de localización, eficiencia de detección, y LS7002

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Introduction

In 2013, Vaisala introduced the LS7002 Advanced Total Lightning sensor. By employing improved embedded software features along with the latest central processing software (the Total Lightning Processor), an LS7002 network can achieve enhanced cloud-to-ground and intracloud (IC) flash detection efficiency. Recently, a network-wide upgrade of the U.S. National Lightning

Detection Network (NLDN) was completed. Prior to this upgrade, the NLDN consisted of 114 LS7001 and IMPACT-ESP (Improved Accuracy through Combined Technology - Enhanced Sensitivity and Performance) sensors, which provided both time of arrival and azimuth information. Currently, all sensors in the NLDN are upgraded to Vaisala's LS7002 technology. In addition, a new geolocation algorithm is being tested and is expected to be implemented in the NLDN central processor in mid-2014. In this paper, we discuss the enhanced features of the LS7002 and the results expected from the current network-wide upgrade on the performance characteristics of the U.S. NLDN. We also examine the peak current distributions of cloud and cloud-to-ground lightning reported by the network.

LS7002 Technology Evolution

The performance characteristics of a lightning detection network depend upon the characteristics of its sensors and the techniques used in the network's central processor to geolocate lightning.

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The LS7002 deploys the latest in digital sensor technology. Additional improvements have been made to the algorithms used in the central processor as well.

Changes that Affect Detection Efficiency

The LS7002 employs the latest digital sensor technology along with improved embedded software with enhanced features. Digital processing improves the sensitivity of the sensor to low amplitude lightning-generated signals by a factor of about 3 as compared to the analog IMPACT-ESP sensor. The LS7002 also transmits additional waveform parameters for each measured lightning event to the central processor. Digital filtering of local noise sources allows better signal-to-noise ratio along with flexibility in site selection. Note that the LS7002, like the IMPACT-ESP and LS7001, measures both timing and angle (direction) information associated with lightning events. This allows the use of a combination of Magnetic Direction Finding and Time of Arrival techniques to geolocate lightning discharges with as few as two sensors. The combined enhancements in sensor sensitivity and embedded sensor software allow detection of low amplitude lightning events (primarily cloud pulses) and are expected to result in a cloud flash detection efficiency of around 40-50% with network baseline distances (distances between adjacent sensors in a network) of 300-350 km.

Additionally, a new lightning location algorithm (referred to herein as “burst processing”) in the central processor will allow the geolocation of multiple pulses in lightning pulse bursts or trains (e.g., Rakov et al., 1996, Nag and Rakov, 2009). It is expected that multiple cloud pulses will be geolocated for each cloud flash in a large fraction of cloud flashes. This will further enhance the cloud lightning detection efficiency of the network by about 6% on average (Murphy and Nag, 2014). Finally, a new lightning classification algorithm that uses multiple waveform parameters to classify cloud and cloud-to-ground lightning with an accuracy of 80-90% has been implemented. Currently, the central processor uses waveform parameters to differentiate between cloud and cloud-to-ground lightning, but it also classifies all positive lightning events having peak currents less than 15 kA as cloud lightning. The new classification algorithm removes this hard limit for peak current for positive events and classifies lightning events solely on the basis of their waveform characteristics. These improvements to the central processor are currently under test and are expected to be deployed in mid-2014.

Changes that Affect Location Accuracy

The LS7002 sensors use waveform onset corrections, which accurately determine the arrival time of electromagnetic waveforms from lightning events at a sensor. This reduces the timing error and improves the accuracy with which lightning events can be geolocated (Honma et al., 2013). The waveform onset corrections have led to an improvement in the median location accuracy (given by the length of the semi-major axis of the 50% error ellipse) of the NLDN from about 300 m to about 200 m in the interior of the network. The location accuracy of the NLDN is evaluated using lightning strikes to towers by Cramer and Cummins (2014). The location accuracy is expected to improve further when additional factors such as propagation across uneven terrain, varying ground conductivity, and improved handling of electromagnetic wave propagation (resulting in smaller arrival time errors) are taken into account in the new central processor (to be implemented in mid-2014).

NLDN Performance Characteristics and Validation

The performance of a lightning detection network is primarily measured by its detection efficiency, location accuracy, peak current estimation accuracy, and type/polarity estimation accuracy for different kinds of lightning discharges. Figure 1 shows the current model estimated cloud-to-ground (CG) lightning flash detection efficiency for the North American Lightning Detection Network, or NALDN, which consists of the Canadian Lightning Detection Network (CLDN) and the U.S. NLDN. The flash detection efficiency is expected to be about 95% for the entire United States. Additionally, the NLDN is expected to have about 40-50% detection efficiency for cloud flashes. Figure 2 shows the current model estimated median location accuracy for the NALDN. The location accuracy is expected to be approximately 150 to 250 m over the majority of the United States, falling to the 250-500 m range toward the edges of the network.

Table 1. Summary of performance characteristics of the NLDN in 2013 evaluated using rocket-triggered lightning (Mallick et al., 2014)

Characteristic	Flashes/Return Strokes
CG Flash detection efficiency	100%
Stroke detection efficiency	76%
Median location accuracy	173 m
Misclassified return strokes	2.1%
Peak current estimation error	15%

These performance characteristics have been validated over the years using a variety of techniques such as tower studies, video camera studies, and triggered lightning studies (e.g., Jerauld et al., 2004, Biagi et al., 2005, Nag et al., 2011). Mallick et al. (2014) examined the performance characteristics of the NLDN for the 2004–2013 period using rocket-triggered lightning data acquired at Camp Blanding, Florida. Table 1 summarizes the NLDN flash and stroke detection efficiencies for 2013 in Florida. The flash and stroke detection efficiencies were 100% and 76%, respectively. The median absolute location error was 173 m, and the median absolute value of current estimation error was 15%. In 2013, 2.1% (one out of 47) of the triggered lightning return strokes (similar to subsequent strokes in natural lightning) was misclassified by the NLDN.

Evaluation of Enhanced Cloud Lightning Detection

The ratio of the number of cloud lightning pulses to the number of cloud-to-ground lightning return strokes detected by a network can serve as a measure of change in the network's cloud lightning detection efficiency from one time period to another if regional, seasonal, and storm-to-storm variations in IC-to-CG ratio are minimized. This is done by calculating the IC-to-CG ratio over the same geographical region for all time periods, taking all time periods from the same season in different years, and taking time periods long enough to contain an adequate number of thunderstorm days. Further, it is important that the network's detection efficiency for CG strokes remains relatively unchanged for the time periods under consideration.

Figure 3 shows the histogram of the hourly IC-to-CG ratio for the May 15 to June 15 period in 2010 (brown bars) and in 2013 (blue bars). Both the 2010 and 2013 datasets are from the U.S. Central Great Plains region within the latitude and longitude bounds of (31, -102) and (42, -93). Note that the upgrade of the NLDN to the new LS7002 technology was ongoing in this region in the May 15-June 15 period of 2013, and hence these results are to be treated as preliminary. The hourly IC-to-CG ratio was approximately in the range of 0.07 to 3.4 for the 2010 data with the arithmetic mean ratio being 0.84. For the 2013 data, the IC-to-CG ratio is approximately in the range of 0.22 to 21 with the arithmetic mean ratio being 4.0. This indicates roughly a factor-of-four increase in the IC-to-CG ratio after the 2013 upgrade and hence an increase in the detection efficiency of cloud lightning pulses by a factor of four under the assumption of constant CG detection efficiency. The CG stroke detection efficiency of the NLDN in 2010 was in the 75-80% range. The enhancements in NLDN sensor sensitivity in 2013 are expected to improve the CG stroke detection efficiency to about 80-85% as a result of increased detection of low-amplitude return strokes. Hence the factor-of-four increase in cloud lightning detection efficiency estimated above may be treated as a lower bound. A more rigorous analysis of the improvement in cloud lightning detection efficiency will be done in the near future using cloud lightning flashes detected by Lightning Mapping Arrays as ground truth, once NLDN data over a longer time period is available.

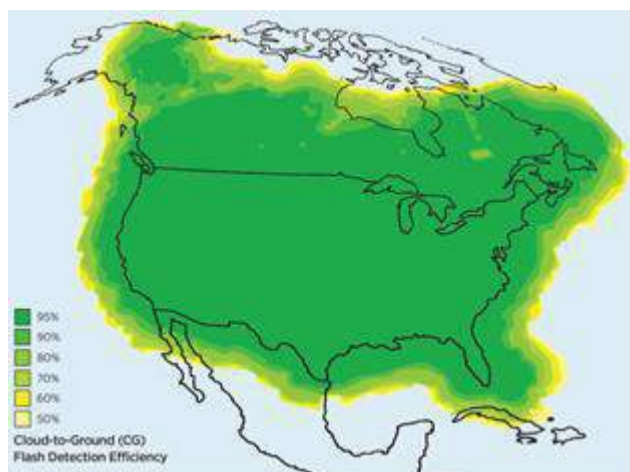


Figure 1. Map showing the model estimated cloud-to-ground flash detection efficiency of the North American Lightning Detection Network.

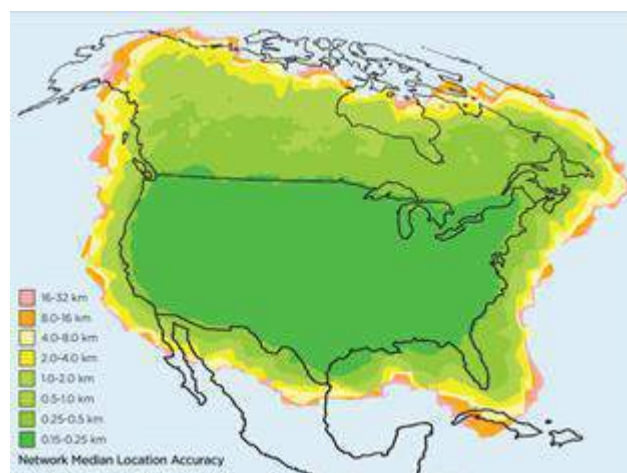


Figure 2. Map showing the model estimated median location accuracy of the North American Lightning Detection Network.

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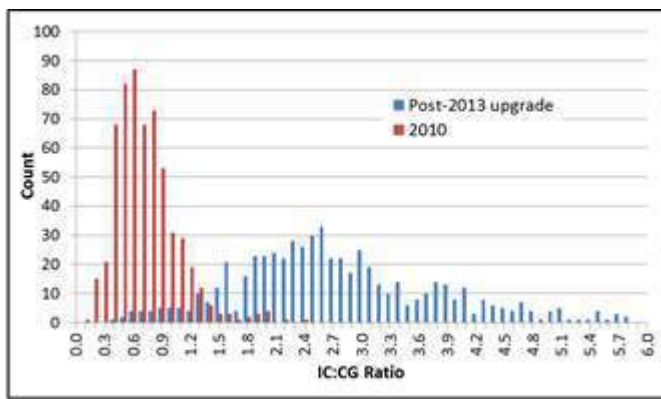


Figure 3. Histogram of the hourly ratio of the number of cloud lightning pulses to cloud-to-ground lightning return strokes detected by the NLDN in 2010 (brown bars) and 2013 (blue bars). Note that the horizontal axis is truncated at an hourly ratio of 6.0 as only 1.4% of the ratios in 2013 were above that value.

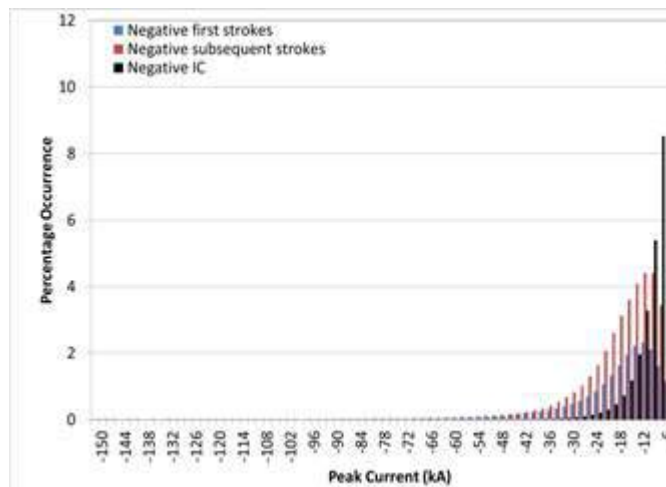


Figure 4. Histogram of NLDN-estimated peak current for negative and subsequent return strokes and cloud pulses shown in 2 kA bins. Note that the horizontal axis is truncated at -150 kA as the number of events having peak currents less than that value is smaller than 0.08%.

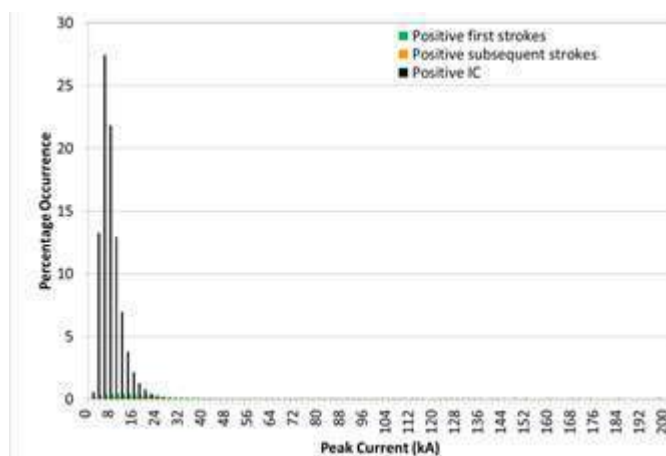


Figure 5. Histogram of NLDN-estimated peak current for positive first and subsequent return strokes and cloud pulses shown in 2 kA bins. Note that the horizontal axis is truncated at 200 kA

as the number of events having peak currents greater than that value is smaller than 0.02%.

Analysis of Lightning Peak Currents

In the following analysis we examine lightning discharges reported by the NLDN in early September to late November, 2013 within the interior of the contiguous United States. About 5.5 million lightning events (CG strokes and cloud pulses) were reported by the NLDN during this period. About 63% of these were cloud pulses as classified by the NLDN. Note that this dataset was obtained by offline reprocessing of the raw data using the new geolocation algorithm (currently under test, as discussed in Section III) and hence includes the new classification technique and “burst processing”. Figures 4 and 5 show the histograms of peak current for negative and positive events, respectively. Note that the horizontal axes in Figures 4 and 5 are truncated at -150 kA and 200 kA, respectively, and the number of events having peak current magnitudes beyond those limits was less than 0.08% and 0.02%, respectively. The number of NLDN-reported negative CG strokes (first and subsequent combined) was comparable to the number of reported negative cloud pulses. On the other hand, for positive events, the large majority (92%) were cloud pulses and less than 10% were first and subsequent strokes.

As noted in Section III, the NLDN peak current estimation error for cloud-to-ground subsequent strokes is 15%. The peak current is estimated using a transmission-line-equivalent model that converts the measured peak magnetic field into peak current. The same field-to-current conversion equation is used for estimating peak currents for cloud pulses as well. However, it is to be noted that the transmission line model may not be applicable for cloud lightning pulses (e.g. Nag et al., 2011), and the NLDN-estimated peak currents should be considered as a quantity proportional to the initial field peak in cloud pulses.

Cloud-to-Ground Lightning Multiplicity and Peak Currents

Of the CG flashes reported by the NLDN during this period, 81% were negative and 19% were positive. The average multiplicity (number of strokes per flash) for negative CG flashes was 2.7 and for positive CG flashes was 1.4. The NLDN flash grouping algorithm allows a maximum of 15 strokes to belong to one flash. Strokes of order greater than 15 are grouped into a separate flash. Additionally, it is possible that a small fraction of cloud pulses were misclassified by the NLDN as single stroke CG flashes and some low peak current subsequent strokes were not reported by the NLDN. Hence, the average multiplicity, especially for negative CG flashes, is likely to be slightly underestimated.

Figures 6 and 7 show the histograms of peak current for negative and positive CG strokes, respectively. The peak currents for negative first strokes ranged from -0.8 kA to -501 kA with the arithmetic mean (AM) and median peak currents being -21 kA and -15 kA, respectively. For negative subsequent strokes, the peak currents ranged from -1.1 kA to -397 kA with the AM and median being -17 kA and -15 kA, respectively. While the peak current distribution for negative first and subsequent strokes looks reasonable, it is likely that some negative leader pulses were misclassified as negative first strokes and some low peak current subsequent strokes were not reported by the NLDN or were misclassified as cloud pulses. Hence, the AM value for negative first strokes may be a slight underestimate (in absolute value) and that for negative subsequent strokes may be a slight

overestimate (in absolute value). The peak currents for positive first strokes ranged from 1.1 kA to 544 kA with the AM and median peak currents being 24 kA and 19 kA, respectively. For positive subsequent strokes, the peak currents ranged from 1.3 kA to 473 kA with the AM and median being 24 kA and 19 kA, respectively. As discussed in Section II, at present, in addition to classifying events based on waveform characteristics, the NLDN classifies all positive lightning events below 15 kA as cloud pulses. In the new algorithm, this lower limit for peak current of positive CG strokes has been removed and only a waveform-based classification is used. The removal of this lower limit can be seen in Fig. 7.

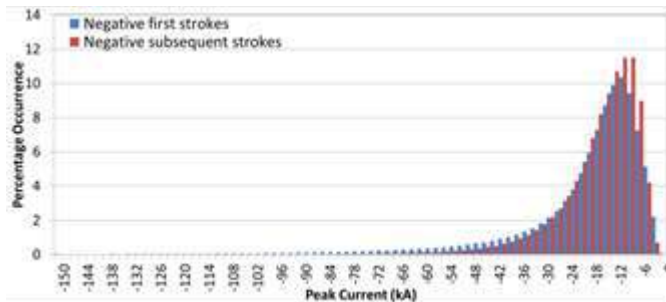


Figure 6. Histogram of NLDN-estimated peak current for negative first and subsequent return strokes shown in 2 kA bins. Note that the horizontal axis is truncated at -150 kA as only a small fraction of the return strokes have peak currents less than that value.

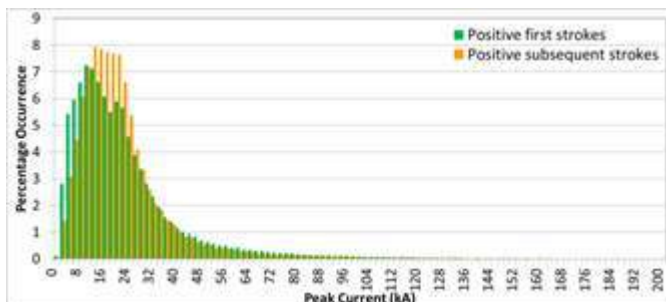


Figure 7. Histogram of NLDN-estimated peak current for positive first and subsequent return strokes shown in 2 kA bins. Note that the horizontal axis is truncated at 200 kA as only a small fraction of return strokes have peak currents greater than that value.

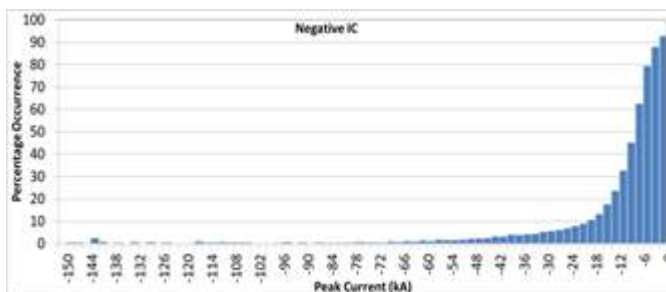


Figure 8. Percentage of NLDN-reported negative lightning events that were cloud pulses shown in 2 kA bins.

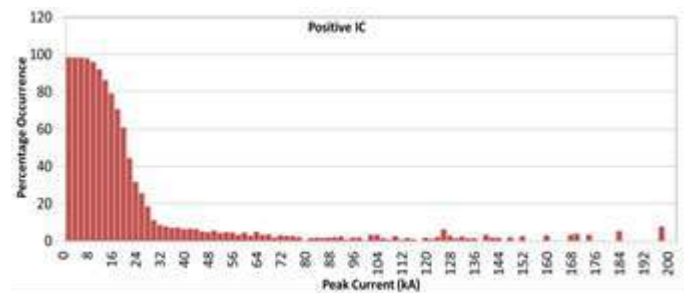


Figure 9. Percentage of NLDN-reported positive lightning events that were cloud pulses shown in 2 kA bins.

Cloud Lightning Peak Currents

In the August to November 2013 period for the area being considered in this study, the large majority (87%) of flashes reported by the NLDN were ICs. In this context, an IC “flash” was defined simply by grouping IC pulses using the same algorithm that is normally applied to CG strokes in the NLDN. Figures 8 and 9 show the percentage of negative and positive events that were cloud pulses. The majority of events with peak current magnitude less than 20 kA for positive events and less than 8 kA for negative events were cloud pulses. Interestingly, a relatively significant fraction of events in higher peak current bins are classified as cloud (e.g., in the 180–182 kA and 196–198 kA ranges in Figure 9), even though the overall number of events in those peak current ranges is small. It is possible that terrestrial gamma ray flashes that produce high-amplitude bipolar pulses are detected by the NLDN and classified as cloud discharges. However, further investigation is necessary in order to determine the nature of these events. The histogram of NLDN-estimated peak current for cloud pulses is shown in Figure 10. There were twice as many positive cloud pulses (produced due to negative charge moving upward or positive charge moving downward) than negative cloud pulses (produced due to negative charge moving downward or positive charge moving upward). The peak currents for NLDN-reported negative IC pulses ranged from -0.8 kA to -238 kA with the AM and median being -7.9 kA and -6.6 kA, respectively. For positive cloud pulses, the peak currents ranged from 0.8 kA to 370 kA with the AM and median being 7.3 kA and 6.4 kA, respectively. The shape of the positive and negative peak current distributions look similar indicating no polarity-dependent bias in the NLDN’s detection efficiency. The peak of the distribution for both positive and negative cloud pulses is in the 4–6 kA absolute range. The detection threshold of the NLDN is in the 1–3 kA range depending upon location of a particular lightning event relative to the NLDN sensors, and hence, the number of events reported by the NLDN in this range is likely an underestimate and the average values for cloud pulse peak currents an overestimate.

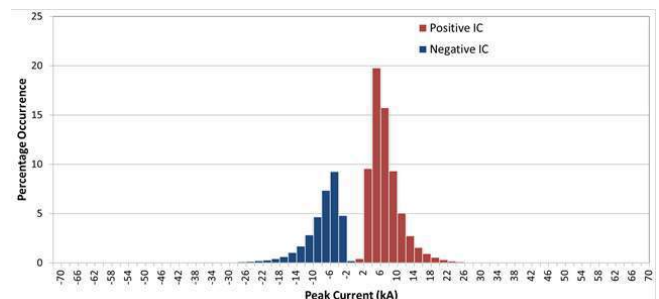


Figure 10. Histogram of NLDN-estimated peak current for positive and negative cloud pulses shown in 2 kA bins. Note that the horizontal axis is truncated at a magnitude of 70 kA at both ends as only a small fraction of cloud pulses have peak currents beyond those limits.

Conclusions

The LS7002 Advanced Total Lightning sensor employs the latest digital sensor technology, which, along with digital filtering of local noise sources, allows better signal-to-noise ratio and improves the sensitivity of the sensor to low amplitude lightning-generated signals. This provides the ability to enhance the detection efficiency for cloud and cloud-to-ground lightning. In 2013, LS7002 sensors were deployed in the U.S. National Lightning Detection Network (NLDN), replacing older generation LS7001 and IMPACT sensors. The cloud flash detection efficiency in the NLDN is expected to be about 40-50%. The hourly IC-to-CG ratio, and hence the number of cloud pulses detected the NLDN, has increased by at least a factor of four as a result of the 2013 upgrade. The location accuracy of the NLDN is expected to be about 200 m in the interior of the network. These performance characteristics continue to be validated by triggered lightning, tower strikes, network inter-comparison, and camera studies.

A new NLDN central processor is expected to be operational in mid-2014. It implements a new "burst processing" algorithm that geolocates multiple pulses in lightning pulse trains. This will further enhance the cloud lightning detection efficiency of the network by about 6% on average. A new lightning classification algorithm that uses multiple waveform parameters to classify cloud and cloud-to-ground lightning with an accuracy of 80-90% will be implemented. Additionally, the NLDN location accuracy is expected to improve further when additional factors such as propagation across uneven terrain, varying ground conductivity, and improved handling of electromagnetic wave propagation (resulting in smaller arrival-time errors) are taken into account in the new NLDN central processor.

We examined lightning discharges reported by the NLDN in early September to late November, 2013 within the interior of the contiguous United States. The majority of lightning events (63%) and flashes (87%) reported by the NLDN were ICs. This is a further indication of a significant improvement in IC detection efficiency. Of the CG flashes reported by the NLDN during this period, 81% were negative and 19% were positive. The average multiplicity for negative CG flashes was 2.7 and for positive CG flashes was 1.4. The negative and positive first stroke median peak current was -15 kA and 19 kA, respectively. The NLDN-reported CG stroke multiplicity and first stroke median peak currents may be slightly underestimated, but they are generally consistent with recent validation studies and the expected accuracy of the new cloud discharge classification algorithm.

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