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Transición energética en la 4ta revolución industrial



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Modeling the Stochastic Security-Constrained Unit Commitment Problem Considering Distribution Shift-Factors

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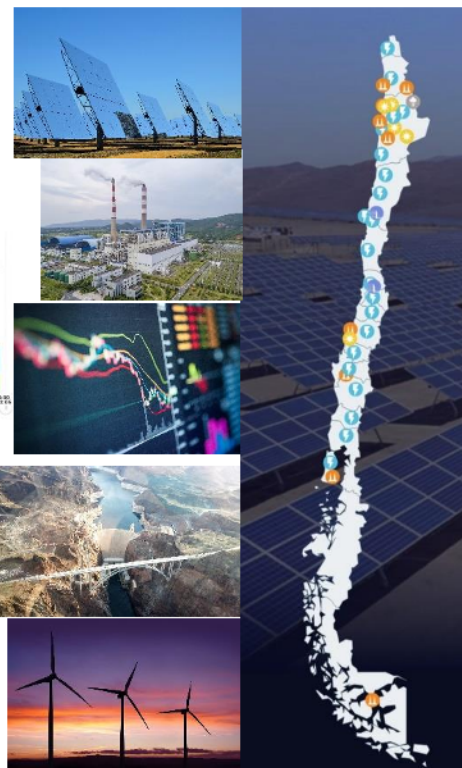
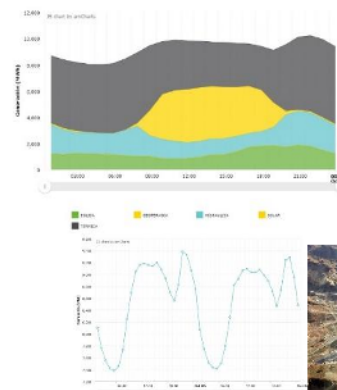
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I. Introduction

UNIT COMMITMENT

Purposes [1]:

- Determine the optimal hourly operation strategy for the generation units for a given horizon.
- Minimizing fuel and starting up and shutting down costs.



I. Introduction

UNIT COMMITMENT
PROBLEM [2]-[4]

MILP o MILQ

OBJECTIVE FUNCION: Minimize total costs.

SYSTEM CONSTRAINTS

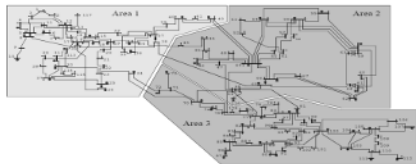
- Spinning Reserve margin.
- System Load Balance.
- Start-up cost.
- Shutdown cost.

BASICAL TECHNICAL CONSTRAINTS

- Power Generation Limits.
- Power Generation Ramp Constraints.
- Minimum Up-Time Generation Constrains.
- Minimum Down-Time Generation Constraints.

NETWORK CONSTRAINS

- Transmission Thermal Limits.



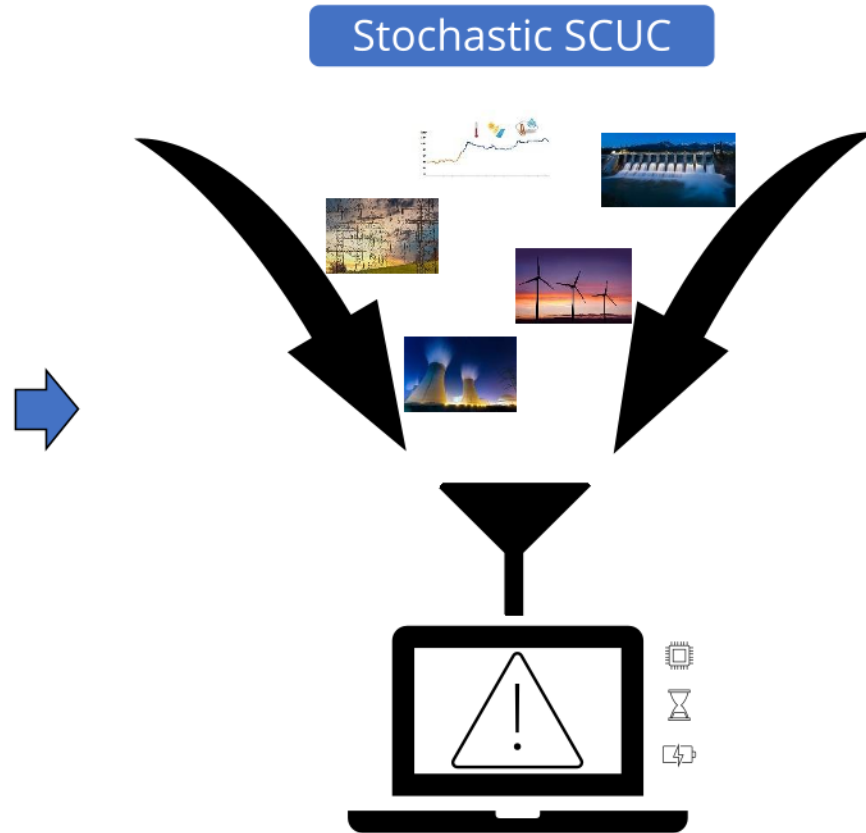
I. Introduction

SECURITY-CONSTRAINED UNIT COMMITMENT

- Transmission capacity.
- Possible contingencies.

STOCHASTIC UNIT COMMITMENT

- Load forecasting.
- Hydro energy availability.
- Fuel prices.
- Renewable energy.



II. Theoretical aspects

Many SCUC uses the classical DC-based formulation to model transmission power flow equations [1].

- Commitment status.
- Production Levels.
- Voltage bus angles (δ_i).

$$(p_{i,t,s} - Pd_{i,t,s}) - \sum_{ij \in L} f_{ij,t,s} = 0$$

$$f_{ij,t,s} = B_{ij} * (\delta_i - \delta_j)$$

$$|f_{ij,t,s}| \leq F_{ij}^M$$

$$|\delta_{i,t,s}| \leq \frac{\pi}{2}$$

$$\forall i \in B, \forall ij \in L, \forall t \in T, \forall s \in S$$

Where:

$p_{i,t,s}$: Active power dispatched

$Pd_{i,t,s}$: Load demand

$f_{ij,t,s}$: Power Flow of Branch ij

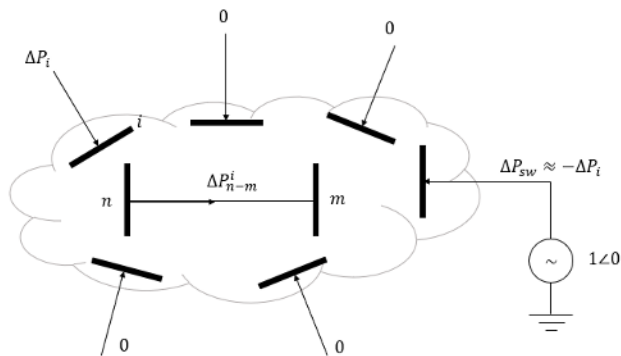
B_{ij} : Susceptance

$\delta_{i,t,s}$: Voltage bus angles

III. Proposed Methodology

Distribution Shift-Factors:

- Gives the variation in flow of line nm due to changes in the nodal injection at bus n .
- SF are a function of transmission susceptance's and the topology.



III. Proposed Methodology

Security Constrained Unit Commitment
SF-based [4]:

- Stochastic mixed-integer problem (SMIP).
- Commitment Status.
- Production Levels.
- No voltage bus angle.

$$\sum_{g \in G} p_{g,t,s} + \sum_{b \in B} ENS_{b,t,s} = \sum_{b \in B} Pd_{b,t,s}$$

$$\left| \sum_{b \in B} SF_{ij,b} * (p_{b,t,s} - Pd_{b,t,s}) \right| \leq F_{ij}^M$$

Where:

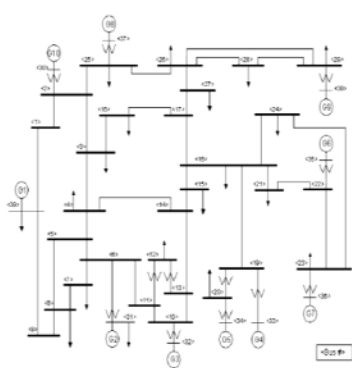
$SF_{ij,b}$: Linear shift-factor for transmission element

IV. Test Power Systems

We use two power systems:

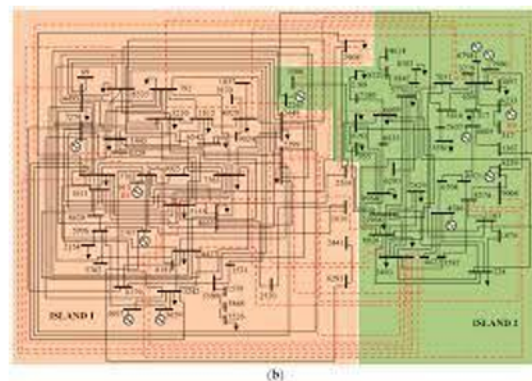
1) IEEE-39 bus [2]

- 10 generators
- 46 branches



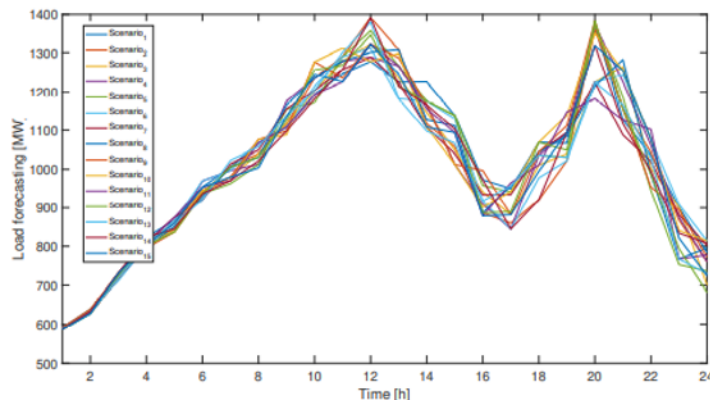
2) Pegase 89-bus

- 12 generators
- 210 branches



15 Synthetic scenarios

- Same probability



V. Simulation Results

STOCHASTIC SCUC – IEEE 39 BUS

- 15 scenarios ($\omega_s = 1/15$).
- 24 hours.
- Reserve margin of 10%.
- Load shedding cost 500 \$/MW.



Intel Core i5 5200 (2.2Ghz) – 8Gb of RAM



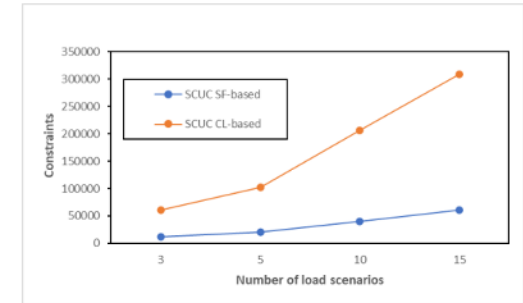
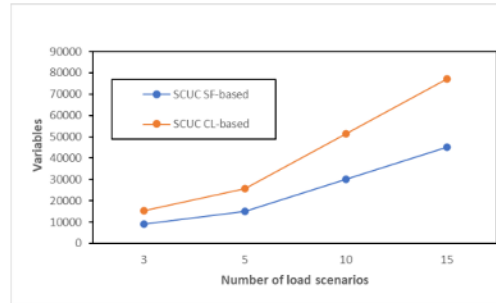
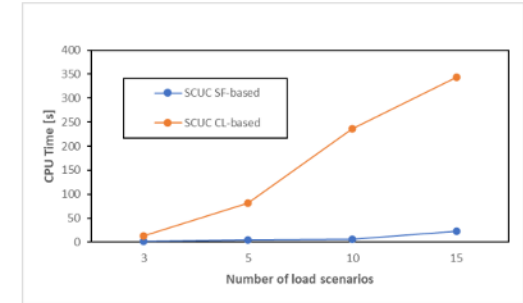
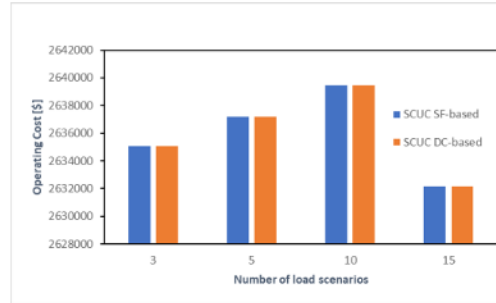
Unit	t1	t2	t3	t4	t5	t6	t7	t8	t9	t10	t11	t12	t13	t14	t15	t16	t17	t18	t19	t20	t21	t22	t23	t24
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
3	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0
4	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0
5	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
6	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	0	0	0	1	1	1	0	0	0
7	0	0	0	0	0	0	0	0	0	0	1	1	1	0	0	0	0	0	0	1	1	1	0	0
8	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
9	1	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	1	0	0	0	0
10	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

T= 24 Hours	SSCUC SF-based	SSCUC Classical
Scenarios	15	15
Operational Cost [\$]	502,072.96	502,072.96
Start up Cost [\$]	5,980.00	5,980.00
Variables	36360	50400
Constraints	51030	126270
Solver Time [s]	47.96	168.9

V. Simulation Results

STOCHASTIC SCUC RESULTS TRANSMISSION CAPACITY – PEGASE 89 BUS

- Including transmission network.
- 3,5,10,15 load scenarios.

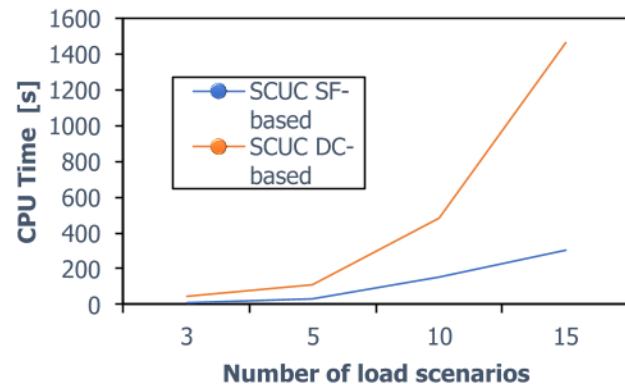
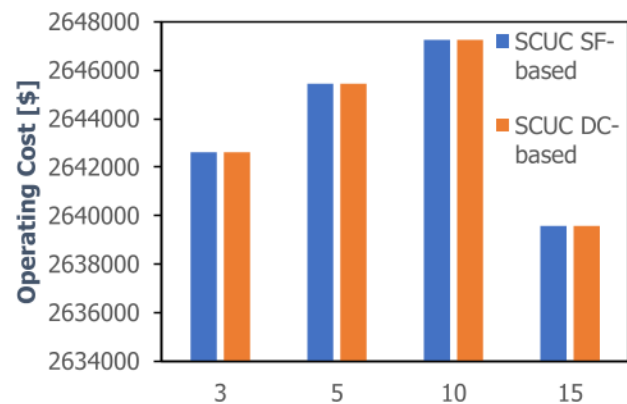


SSCUC SF based is more compact and less computationally burdensome.

V. Simulation Results

STOCHASTIC SCUC RESULTS INCLUDING
A LOWER TRANSMISSION CAPACITY –
PEGASE 89 BUS

- We reduced transmission network capacity.
- Include load scenarios (3-5-10-15)



VI. Conclusions

This study introduced an efficient SCUC formulation based on shift-factors to cope with the stochastic UC problem. Simulation results showed a very significant reduction in problem size and simulation time achieved by the SF-based formulation in comparison with the classical formulation without compromising the solution's optimality.

VII. References

- [1] A. J. Wood and B. F. Wollenberg, Power Generation, Operation and Control. John Wiley & Sons, 1996.
- [2] M. Carrion and J. M. Arroyo, "A computationally efficient mixed-integer linear formulation for the thermal unit commitment problem," IEEE Transactions on Power Systems, vol. 21, no. 3, pp. 1371–1378, 2006.
- [3] J. Birge and F. Louveuax, Introduction to Stochastic Programming. ser. Springer Series in Operations Research and Financial Engineering, Springer-Verlag, 2011.
- [4] V. Hinojosa and F. Gonzalez-Longatt, "Stochastic security-constrained generation expansion planning methodology based on a generalized line outage distribution factors," in 2017 IEEE Manchester PowerTech, 2017, pp. 1–6.

VIII. Questions



THANKS