Straight-Line Conventional Transient Pressure Analysis for Horizontal Wells with Isolated Zones

Análisis Convencional de Pruebas de Presión en Pozos Horizontales con Zonas Aisladas

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Abstract

It is common in the oil industry to complete horizontal wells selectively. Even, this selection is performed naturally since reservoir heterogeneity may cause segmented well performance. Segmentation may be partially open to flux due to high skin factor or low permeability bands. They can be treated as a nonuniform skin distribution. A few models have been introduced to capture these special details. Existing interpretation methodologies use non-linear regression analysis and the TDS technique; but, there is an absence of equations for the conventional technique. In this study, the conventional methodology is developed for the analysis of pressure transient tests in horizontal wells with isolated zones so directional permeabilities and skin factors can be obtained. The developed expressions were tested successfully with several examples reported in the literature and compared to results from other sources.

Key Words: Horizontal well, isolation zones, partial completion, flow regimes.

Resumen

Es común en la industria petrolera completar los pozos en forma selectiva. Incluso, dicha selección se efectúa de forma natural ya que la heterogeneidad del yacimiento podría causar comportamiento segmentado del pozo. La segmentación podría estar parcialmente abierto al flujo en virtud al alto factor de daño bajas vetas de permeabilidad. Ellas pueden tratarse como una distribución no uniforme del factor de daño. Algunos pocos modelos se han introducido para capturar estos detalles especiales. Las metodologías de interpretación existentes usan análisis de regresión no lineal y la técnica TDS, pero, se adolece de ecuaciones para el método convencional. En este estudio se desarrolla la metodología convencional para la interpretación de pruebas de presión en pozos horizontales con zonas aisladas de modo que se puedan estimar las permeabilidades y los factores de daño. Las expresiones desarrolladas se probaron satisfactoriamente con varios problemas encontrados en la literatura y se compararon con los resultados procedentes de otras fuentes.

Palabras clave: Pozo horizontal, zonas aisladas, completamiento parcial, regímenes de flujo.

1. Introduction

Selective completion is a current operation performed on horizontal wells. Reservoir heterogeneity may also cause segmentation due to low permeability bands [1]. As indicated by [1], [2] and [3] the existence of an intermediate late radial or pseudoradial flow regime is the most important feature of the transient-pressure response of segmented horizontal wells. They found that the semilog slope of the late radial flow regime is affected by the number of equal-length segments.

Horizontal wells with isolated areas can be a practical solution for such problems presented in different formations such as gas/water coning, sand production and asphalt production; however, it has a great impact in the skin factor. Currently, the characterization of locations is important since it is a valuable tool which allows for the determination of the best exploitation scenario.

Recently, [4] introduced a new model for the type of geometry here discussed. They made a detailed discussion of the importance and impact of selective horizontal well completion. Also, they formulated the TDS methodology, initially introduced by [5] for horizontal wells, for interpretation of well pressure tests in segmented horizontal wells. In this study, the solution proposed by [4] is used to develop equations to be used in the conventional straight-line methodology and successfully applied to field examples provided by [4] and [6]. The results of the estimated permeabilities in the x and z directions and skin factors were compared with those from [4] using the TDS technique. Escobar et al. [7] have indicated the importance of the traditional-convventional analysis even in transient-rate tests interpretation.
So far, the only available methodology for well test interpretation in the systems under consideration was the one presented by [4] following the philosophy of the TDS technique [8]. However, the importance of its application is based upon some examples recently reported in the literature. For instance, [9] presented some examples for the use of zonal isolations in horizontal well completions in a hydraulic fracturing treatment which was conducted with five packer isolation systems so that five isolated zones were created. On the other hand, [10] introduced some field examples for well testing procedures in multi-zone openhole completion wells in which casing annulus packers, instead of cement, were used to provide the isolations.

2 Formulation

2.1. Mathematical Model

The model developed by [1] corresponds to the dimensionless pressure governing equation based upon the following assumptions: (1) homogeneous reservoir, with constant and uniform thickness with closed top and bottom boundaries. (2) Anisotropic system but with constant porosity and permeability in each direction, (3) negligible frictional and gravitational effects, and (4) the well extends in the midpoint of the formation height.

\[ P_D(x_D, y_D, z_D, t_D) = \frac{x_D}{L_w} \int \frac{\tau_0}{2\pi L_w} \times \left[ \sum_{n=1}^{\infty} \left[ \frac{X_0}{2\pi L_w} \right]^2 \frac{e^{-x_D^{2}/2\pi L_w}}{\sqrt{\pi L_w}} \times \left[ 1 + 2 \sum_{b=1}^{\infty} e^{-x_D^{2}/2\pi L_w} \cos(N\pi z_D) \cos(N\pi (y_D + z_D)) \right] dt_D \right] \]

In which the dimensionless parameters are as follows:

\[ x_D = \frac{x - x_w}{L_w} \]

\[ y_D = \frac{y - y_w}{L_w} \sqrt{\frac{k_s}{k_x}} \]

\[ z_D = \frac{z - z_w}{L_w} \sqrt{\frac{k_s}{k_z}} \]

\[ z_{D,n} = \frac{z_{nL}}{h} \]

\[ z_D = \frac{z - z_w}{h} = z_D L_D \]

\[ L_D = \frac{L_w}{h} \sqrt{\frac{k_z}{k_x}} \]  \hfill (7)

\[ L_{w,D} = \frac{L_w}{L_w} \]  \hfill (8)

\[ L_{p,D} = \frac{L_p}{L_w} \]  \hfill (9)

\[ t_D = \frac{k_t}{\phi \mu c_i L_w} \] \hfill where: \[ \eta_s = \frac{k_s}{\phi \mu c_i} \]

\[ P_D(x_D, y_D, z_D, t_D) = \frac{2\pi \sqrt{k_t h \Delta P_{[x,y,z]}}}{\phi \mu B} \]  \hfill (11)

2.2. General equation of horizontal wells with isolated zones

Flow regimes in horizontal wells depend upon several issues mainly related to geometry. When the ratio of the wellbore length to the reservoir thickness, LD, is less than 5 the well acts a single source/sink, then, early spherical flow develops. As example of such case is sketched in Fig. 1. If LD becomes larger than 20 then early-radial flow cannot be seen since the formation thickness results too thin compared to the wellbore length and the top and bottom of the formation are quickly reached.

As stated before, radial flow regime develops in short horizontal wells (LD=20) with or without isolated zones. The governing expression presented by [4] is given by:

\[ P_D = \frac{1}{4nL_{w,D}L_D} \left[ \ln \left( \frac{t_D}{y_D^2 + z_D^2} \right) + 0.80907 \right] + s_{m,n} \frac{L_w}{nL_{w,D}L_D} \]

\[ Ei \left( -\frac{y_D^2 + z_D^2}{4t_D} \right) \leq 0.01 \]  \hfill (12)

When Z=0, Equation 12 becomes:

\[ P_D = \frac{1}{4nL_{w,D}L_D} \left[ \ln \left( \frac{t_D}{y_D^2 + z_D^2} \right) + 0.80907 + 4s_{m,n} \right] \]  \hfill (13)

Figure 1. Spherical flow regime in an a horizontal well with selective completion.
Replacing the dimensionless quantities in Equation (13), dividing by the natural log of 10 and solving for the well-flowing pressure, it yields:

\[ P_{wf} = P_i - \frac{81.28q\mu B}{nl_nk_z} \times \left( \log \frac{t}{\phi\mu c_i \left( r_n/\sqrt{k_z} \right)^2 + (z-nL/k_z)^2} - 3.2275 + 4s_m \right) \]  

(14)

The slope, \( m_{ER} \), from a semilog plot of pressure versus time allows for the estimation of \( (k_xk_y)^{0.5} \),

\[ \sqrt{k_xk_y} = \frac{81.28q\mu B}{nl_n m_{ER}} \]  

(15)

The sketch of Fig. 2 shows the development of an intermediate radial flow when a horizontal well possesses isolated zones indicating that 5 < \( L_D < 20 \). The governing dimensionless pressure derivative equation for such flow regime is:

\[ (t_D \ast P_{D'}) = \frac{0.5}{n} \]  

(16)

Since the semilog slope is natural log of 10 times higher than the pressure derivative value, Equation (16) allows one to find an expression to find the horizontal permeability, \( (k_xk_y)^{0.5} \) from the semilog slope, \( m_{ER} \), once the dimensionless pressure derivative is placed in oilfield units;

\[ \sqrt{k_xk_y} = \frac{162.6q\mu B}{nh m_{ER}} \]  

(17)

As described by Fig. 3, the pseudo-spherical (or two hemispherical) flow develops when the length of the perforated area is so short compared to the formation thickness forcing the well to act as a single source/sink. The dimensionless pressure derivative governing equation presented by [4] is:

\[ (t \ast P_{D'})_{op} = \frac{1}{4\sqrt{\pi t_D}} \]  

(18)

Integration of the Equation (18) leads us to obtain the dimensionless pressure for such flow regime:

\[ P_D = \frac{1}{2\sqrt{\pi t_D}} + s_{ps} \]  

(19)

Replacing the dimensionless terms, we obtain:

\[ \sqrt{k_xk_y h\Delta P} = \frac{1}{141.2q\mu B} \times \frac{1}{2\sqrt{\pi \times 0.0002637k_x t}} + s_{ps} \]  

(20)

The slope of a Cartesian plot of pressure versus the inverse square root of time, mps, allows one to calculate \( k_x(0.5) \), knowing mps of a Cartesian graph.

\[ k_x = \frac{2453q\mu B L_w}{hm_{ps} \sqrt{k_y t}} \]  

(21)

Needless to say that the pseudo-spherical skin factor can be obtained from the intercept of such a plot.

In long horizontal wells (\( L_D > 20 \)), the early radial flow regime is hardly seen while early linear flow is dominant in the proximities to the well. The governing dimensionless pressure derivative equation for this linear flow is given by [4],

\[ (t_D \ast P_{D'})_{EL} = \sqrt{\frac{\pi t_D}{2nL_{op}}} \]  

(22)

Integration of Equation 22 leads to the dimensionless pressure governing equation;

\[ P_D = \frac{\sqrt{\pi t_D}}{nL_{op}} + s_i \]  

(23)

After replacing the dimensionless quantities, we obtain:

\[ \sqrt{k_x h\Delta P} = \frac{4.064}{q\mu B} \times \frac{t}{\phi\mu c_i \sqrt{k_y t}} + s_i \]  

(23)

Equation (23) suggests that a plot of pressure versus the square root of time provides a straight line whose slope \( m_{EL} \) can be used to estimate the square root of \( k_y \),
Figure 4. System of early linear flow for long horizontal wells with a high number of isolated zones, after [6]

\[
\sqrt{k_y} = \frac{4.064q\mu B}{nL_p h m_{EL}} \sqrt{\frac{t}{\mu c_i}}
\]  

(24)

Fig. 4 shows that once early-radial flow vanishes, the well acts as a hydraulic fracture, then linear flow develops. A long horizontal well \((L_D>20)\) with a high number of isolated zones also exhibits an early linear flow regime which is effective to the whole wellbore. The dimensionless pressure derivative governing equation was presented by [4] as follows:

\[
(t_D * P_D')_{EL} = \frac{\sqrt{\pi t_D}}{2nL_D}
\]  

(25)

After integration of Equation 25, we obtain:

\[
P_D = \sqrt{\pi t_D} \frac{1}{nL_D} + s_i
\]  

(26)

Once the dimensionless terms are replaced the expression for the dimensionless pressure is presented:

\[
\sqrt{k_y h P_i q \mu B} = \frac{4.064}{nL_D} \frac{1}{\phi c_i} + s_i
\]  

(27)

A plot of pressure versus the square root of time should be a straight line which slope, \(m_{EL}\), allows the estimation of \(k_y^{0.5}\).

\[
\sqrt{k_y} = \frac{4.064q\mu B}{nL_p h m_{EL}} \sqrt{\frac{1}{\phi c_i}}
\]  

(28)

At later time, the pseudoradial or late radial flow regime develops in the horizontal plane without any influence of the vertical permeability. See Fig. 5. The dimensionless pressure governing equation was also introduced by [4] as follows:

\[
P_D(x_D, y_D, z_D, t_D) = \frac{1}{2} \left[ \ln t_D + \frac{2s_y}{L_{pD} L_D} \right]
\]  

(29)

In oilfield units,

\[
P_{el} = P_i - \frac{162.6q \mu B}{k_x k_y h} \left[ \log \left( \frac{k_t}{\phi c_i k_y} \right) + \frac{0.8686x_i h}{L_x} \frac{3.5789}{k_y} \right]
\]  

(30)

This flow regime corresponds to the radial flow regime observed in vertical wells. The dimensionless pressure derivative equation is:

\[
(t_D * P_D' )_{pr} = 0.5
\]  

(31)

Equation (31) is useful to calculate the horizontal permeability \((k_x k_y)^{0.5}\) if the semilog slope of a plot of pressure versus time, \(m_{pr}\), is estimated during this flow regime, as:

\[
\sqrt{k_y} = \frac{162.6q \mu B}{h m_{pr}}
\]  

(32)

Such later flow regimes as late linear and pseudosteady state are similar to conventional horizontal wells.

Different expressions to estimate the skin factors are provided in Appendix A.

3. Examples

Example 1 was taken from [4]. Examples 2 and 3 were taken from [6]. In both cases the examples were worked by the TDS technique.

3.1. Example 1

Fig. 6 presents pressure and pressure derivative data for a pressure drawdown test run in a horizontal well having two equal-length isolated zones, each of 400 ft. Other known reservoir and well data are:

\[
q = 500 \text{ STB/D} \quad \phi = 0.05 \quad \mu = 0.5 \text{ cp}
\]

\[
c_i = 1\times10^6 \quad \text{psi}^{-1} \quad h = 62.5 \text{ ft} \quad L_m = 2000 \text{ ft}
\]

\[
r_w = 0.5 \text{ ft} \quad P_i = 4000 \text{ psi} \quad L_v = 2\times400 \text{ ft}
\]

\[
B = 2\times600 \text{ ft} \quad B = 1.2 \text{ bbl/STB}
\]

\[
n = 2
\]

Estimate formation permeability in all directions using the conventional technique.
3.2. Example 2

The pressure and pressure derivative data for a drawdown test of a horizontal well are given in Fig. 10. Other relevant data are given as follows:

\[
\begin{align*}
q &= 4000 \text{ BPD} \\
P_i &= 5000 \text{ psia} \\
L_m &= 4000 \text{ ft} \\
\phi &= 0.1 \\
c &= 0.000002 \text{ psi}^{-1} \\
B &= 1.125 \text{ rb/STB} \\
r_m &= 0.566 \text{ ft} \\
h &= 125 \text{ ft} \\
\mu &= 1 \text{ cp} \\
n &= 2 \\
L_p &= 800 \text{ ft} \\
k_z &= 8 \text{ md}
\end{align*}
\]

Solution. Early radial, early linear, intermediate radial and pseudoradial flow regimes are clearly seen in the pressure derivative curve of Fig. 10. A slope, \(m_{PR}\), of 80.92 psi/cycle is obtained from the semilog plot given in Fig. 11 which allows to estimate a \((k_zk_y)^{0.5}\) value of 2.82 md using Equation 15. Then, using a slope of 100.68 psi/hr\(^{0.5}\) read from Fig. 12, a \(y\)-direction permeability of 4.12 md is obtained by means of Equation 24. \(k_z\) is readily found from \((k_zk_y)^{0.5}\) and \(k_y\) to be 1.94 md.

Solution. Three flow regimes are clearly seen in Fig. 6: early radial, early linear and pseudoradial. A semilog slope \(m_{PR}\) of 448 psi/cycle is found from Fig. 7 during the late radial flow regime. Equation 32 allows estimating a horizontal permeability, \((k_zk_y)^{0.5}\) of 0.87 md. The Cartesian plot of pressure versus the square root of time given in Fig. 8 provides a slope, \(m_{EL}\), of 82 psi/hr\(^{0.5}\). Using Equation 24 a value of \(k_z\) of 1.57 md is found. Knowing \((k_zk_y)^{0.5}\) and \(k_z\), a value of \(k_y\) of 0.49 md is readily obtained. From Fig. 9, a semilog slope, \(m_{ER}\), of 23 psi/cycle during the early radial flow regime is used to calculate a value of \((k_zk_y)^{0.5}\) of 0.88 md using Equation 17. From this, a value of 0.49 for \(k_z\) is then found.

Figure 6. Log-log plot of pressure and pressure derivative vs. time for example 1. After [4]

Figure 7. Semilog plot of pressure vs. time during pseudoradial flow regime for example 1

Figure 8. Cartesian plot of pressure vs. the square root of time for example 1 (early linear flow)

Figure 9. Semilog plot of pressure vs. time during early radial flow regime for example 1

\((k_zk_y)^{0.5}\)
3.3. Example 3

Figure 13 contains the pressure and pressure derivative data form a drawdown test of a horizontal well presented by [6].

Reservoir, fluid and well parameters are given below:

\[ q = 1000 \text{ BPPD} \]
\[ L_w = 6000 \text{ ft} \]
\[ \phi = 0.1 \]
\[ r_w = 0.7 \text{ ft} \]
\[ \mu = 1 \text{ cp} \]
\[ L_p = 450 \text{ ft} \]

\[ P_i = 5000 \text{ psi} \]
\[ c_r = 0.000002 \text{ psi}^{-1} \]
\[ B = 1.25 \text{ bbl/STB} \]

\[ h = 53 \text{ ft} \]
\[ n = 4 \]

\[ k_x = 20.9 \text{ md} \]
\[ k_z = 15.04 \text{ md} \]

Solution. From the pressure and pressure derivative log-log plot of Fig. 13 the early linear and pseudoradial flow regimes are clearly observed. The semilog slope during the pseudoradial flow regime, Figure 14, \( m_{PR} = 54.08 \text{ psi/cycle} \), leads to the estimation of a horizontal permeability value \((k_k)0.5\) of 17.73 md. A Cartesian slope during linear flow, \( m_{EL} = 30.71 \text{ psi/hr}0.5 \), obtained from Fig. 15 is used to estimate a \( k_y = 15.04 \text{ md} \) from Equation 24. \( k_x \) is then estimated to be 20.9 md.

Table 1. Comparison of results

<table>
<thead>
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<th>Example</th>
<th>Parameters</th>
<th>This Study</th>
<th>TDS - Reference</th>
<th>% error</th>
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<td>0.5 [1]</td>
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<tr>
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<tr>
<td></td>
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<td>4.02 [2]</td>
<td>2.49</td>
</tr>
<tr>
<td>3</td>
<td>( k_x ), md</td>
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<td>15.14 [2]</td>
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</tbody>
</table>
5. CONCLUSION

The straight-line conventional method for pressure-transient analysis was complemented with new equations for horizontal wells with isolated zones. The equations were successfully applied to examples reported in the literature and provided similar results to the TDS technique.

Nomenclature

- $B$: Oil formation factor, rb/STB
- $b_i$: Well position inside the reservoir
- $c_i$: Total system compressibility, 1/psi
- $h$: Formation thickness, ft
- $k$: Permeability, md
- $L$: Total horizontal well length, ft
- $L_o$: Ratio of the horizontal wellbore length to the reservoir thickness $L_o/h$
- $L_P$: Perforated zones length, ft
- $L_z$: Isolated zones length, ft
- $m$: Slope
- $N$: An integer from 1 to infinite. For practical purposes from 1 to 100
- $n$: Number of horizontal-well sections
- $P_i$: Initial reservoir pressure, psi
- $P_{wf}$: Well-flowing pressure, psi
- $P$: Pressure, psi
- $s$: Skin factor
- $q$: Flow rate, BPD
- $t$: Time, hr
- $z$: Well position along the $z$-axis
- $z_0$: Dimensionless well position along the $z$-axis
- $z_w$: Distance from wellbore to formation bottom

Greek

- $\Delta$: Change, drop
- $\phi$: Porosity
- $\mu$: Oil viscosity, cp
- $\tau$: Integration variable - time

Suffices

- $D$: Dimensionless
- $EL$: Early linear
- $ER$: Early radial
- $ps$: Pseudo-spherical
- $int$: Intercept
- $IR$: Intermediate radial
- $m$: Mechanical
- $PR$: Pseudoradial or late radial
- $t$: Total
- $x,y,z$: Coordinates

Appendix A. Skin factor Equations

The mechanical skin factor from Equation 14 is:

$$s_m = \frac{\Delta P_{int} n_{rad} \sqrt{k_x k_z}}{325.12 q \mu B} + 0.8068$$ (A.1)

The pseudo-spherical skin factor from Equation 20 is:

$$s_{ps} = \frac{141.2 q \mu B}{\sqrt{k_x k_z h \Delta P_{int}}}$$ (A.2)

The total skin factor from Equation 23 is:

$$s = \frac{\sqrt{k_x h \Delta P_{int}}}{q \mu B}$$ (A.3)

The total skin factor from Equation 30 is:

$$L_P \left( \frac{\Delta P_{int} \sqrt{k_x k_z h}}{162.6 q \mu B} + 3.5789 \right)$$ (A.4)

References


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